Rail-to-Rail Op Amps

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Rail-to-Rail Op Amps

- There are 2 basic configurations for Op Amp applications:
  (a) inverting configuration, and,
  (b) non-inverting configuration.

(a) Inverting Configuration

(b) Non-Inverting Configuration

(c) Voltage Follower
   (a special case of non-inverting configuration)
Why Rail-to-Rail Differential Input Stage?

• The input and output swings of inverting and non-inverting configurations

<table>
<thead>
<tr>
<th>Configuration</th>
<th>Input common mode voltage swing</th>
<th>Output voltage swing</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inverting</td>
<td>≈0</td>
<td>Rail-to-rail</td>
</tr>
<tr>
<td>Non-inverting</td>
<td>( R_1/(R_1+R_2) \times V_{\text{sup}} )</td>
<td>Rail-to-rail</td>
</tr>
<tr>
<td>Voltage follower</td>
<td>Rail-to-rail</td>
<td>Rail-to-rail</td>
</tr>
</tbody>
</table>

• From the table, we see that for inverting configuration, rail-to-rail input common mode range is not needed. But for non-inverting configuration, some input common mode voltage swing is required, especially for a voltage follower which usually works as an output buffer, we need a rail-to-rail input common mode voltage range! To make an Op Amp work under any circumstance, a differential input with rail-to-rail common mode range is needed.
How to Obtain a Rail-to-Rail Input Common Mode Range?

- We know that usually the input stage of an op amp consists of a differential pair. There are two types of differential pairs.

(a) P-type differential input stage

(b) N-type differential input stage
How to Obtain a Rail-to-Rail Input Common Mode Range? (cont’d)

- First, let us observe how a differential pair works with different input common mode voltage
  - P-type input differential pair

\[
\begin{align*}
V_{\text{CMR}} &= V_{\text{dsat}} + V_T \\
V_{\text{GS}} &= V_{\text{GS},M1,2} \\
I_{\text{tail}} &= \text{gm} \\
I_b &= \text{Input common mode voltage range}
\end{align*}
\]
How to Obtain a Rail-to-Rail Input Common Mode Range? (cont’d)

- N-type differential input stage

![Diagram showing input common mode voltage range with labels for $V_{\text{dsat}}$, $V_{\text{GS}}$, $V_{\text{CMR}}$ (Common Mode Range)].
Why not connect these two pairs in parallel and try to get a full rail-to-rail range? Yes, this is one way!

- There should be an overlap between $V_{CMR,P}$ and $V_{CMR,N}$, so the minimum power supply voltage requirement is
  
  $$(4V_{dsat} + V_{TN} + V_{TP})$$

- $V_{SUP} \geq 4V_{dsat} + V_{TN} + V_{TP}$
How to Obtain a Rail-to-Rail Input Common Mode Range? (cont’d)

- Transconductance vs. Vicm

Region I. When Vicm is close to the negative rail, only P-channel pair operates. The N channel pair is off because its $V_{GS}$ is less than $V_T$. The total transconductance of the differential pair is given by $g_{mT} = g_m$.

Region II. When Vicm is in the middle range, both of the P and N pairs operate. The total transconductance is given by $g_{mT} = g_{mN} + g_{mP} = 2g_m$.

Region III. When Vicm is close to the positive rail, only N-channel pair operates. The total transconductance is given by $g_{mT} = g_{mN} = g_m$.

The total transconductance of the input stage varies from $g_m$ to $2g_m$, the variation is **100%**!
Why is a Constant Gm needed?

- The total transconductance, $g_{mT}$, of the input stage shown in the previous slide varies as much as twice for the common mode range!
- For an operational amplifier, constant transconductance of the input stage is very important for the functionality of the amplifier.
- As an example, we will analyze a simple 2-stage CMOS operational amplifier. The conceptual model of the amplifier is shown below.
Why is a Constant Gm needed? (cont’d)

• The transfer function of the amplifier is given by

\[ A(s) \approx \frac{g_{m1}g_{m2}(1-s\frac{C_m}{g_{m2}})}{s^2C_LC_m + sC_mg_{m2} + g_{o1}g_L} = A_0\frac{1-s\frac{1}{z}}{s^2\frac{1}{p_1p_2} + s\frac{1}{p_1} + 1} \]

where \( A_0 = \frac{g_{m1}g_{m2}}{g_{o1}g_L} \), which is the DC gain of the amplifier.

\[ p_1 = \frac{GBW}{A_0} = \frac{g_{m1}/C_m}{A_0}, \quad p_2 = \frac{g_{m2}}{C_L}, \quad \text{and} \quad z = \frac{g_{m2}}{C_m}, \]

\( p_1 \) and \( p_2 \) are the dominant pole and non-dominant pole of the amplifier respectively, and \( p_1 \ll p_2 \).

\( z \) is the zero generated by the direct high frequency path through \( C_m \).
**Why Should We Have a Constant Gm (cont’d)**

*GBW* is the Gain BandWidth product, or the unity gain frequency of the amplifier, which is given by

\[ GBW = \frac{g_{m1}}{C_m}. \]

We may notice that \( GBW \) changes with \( g_{m1} \)! If \( g_{m1} \) changes 2 times, the \( GBW \) also does so!

- To ensure the stability of the amplifier, we should maintain a sufficient phase margin. Usually, we let \( p_2 \) to be 2.5 times of \( GBW \). Let’s assume \( C_m = C_L/2 \), then \( z = 2p_2 = 5 \times GBW \).

- If the total transconductance of the input stage, \( g_{m1} \), varies 2 times as we have encountered in previous discussion, from \( gm \) to \( 2gm \), let us check what will happen…
Why is a Constant Gm needed? (cont’d)

- We can change $g_m$ by varying some parameters of the input stage. Let us assume that we design an amplifier with sufficient phase margin when $g_{m1}$ is low (which is now $g_m$). That is

$$p_2 = \frac{g_{m2}}{C_L} = 2.5GBW_{LOW} = 2.5 \frac{g_{m1,LOW}}{C_m} = 2.5 \frac{g_m}{C_m},$$

- When $g_{m1}=g_m$, we can get that the phase margin as $57^\circ$, which is sufficient to ensure the stability of the amplifier.
- When the $g_{m1}$ is at its maximum value, $2g_m$, the $GBW$ doubles, at this point, the phase margin changes to $29^\circ$! It is not enough and the amplifier may be unstable and may become an oscillator!!

- Of course we can do in another way that, when $g_{m1}$ is $2g_m$, we design the amplifier with sufficient phase margin, which means,

$$p_2 = \frac{g_{m2}}{C_L} = 2.5GBW_{HIGH} = 2.5 \frac{g_{m1,HIGH}}{C_m} = 5 \frac{g_m}{C_m},$$
We have to push $g_{m2}$ to 2 times of its original value in previous case! It means **more power**, and may reach near the limitation of the process, that is we can only design an amplifier with **50% of the GBW** that a specific process permits. Of course, we do not want either of these two!

- So, transconductance variation of input stage is not desirable, it prevents the optimal frequency compensation of the amplifier. There are other negative effects of the changing transconductance. For instance, $g_m$ variation may introduce extra harmonic distortion because of the changing voltage gain.
  - Let us consider a feedback voltage amplifier with input $g_m$ variation. As shown in the next slide.
  - Assume the open loop gain of the Op Amp is $A_{OL}(s)$, and the transfer function of feedback branch is $H_{FB}(s)$. The close loop gain of the amplifier is defined by
For the practical case, close loop gain of the amplifier in the right figure is given by

\[ A_{CL}(s) = \frac{1}{H_{FB}(s) + \frac{1}{A_{OL}(s)}} \]

- For the practical case, close loop gain of the amplifier in the right figure is given by
  \[ A_{CL}(s) = \frac{1}{H_{FB} + \frac{1}{A_{OL}(s)}} \]

  where \( H_{FB} = \frac{R_2}{R_1 + R_2} \).

- \( A_{CL}(s) \) changes if \( A_{OL}(s) \) varies with the input voltage, although to a less extent, which will introduce some nonlinear distortion at the output, especially at higher frequencies when \( A_{OL}(s) \) is low.
• In summary, we need a **constant** transconductance for the input stage!

• In the following, we will study some structures of constant-gm N-P complementary input stage.
Techniques for N-P Complementary Rail-to-Rail Input Stage

There are several constant gm rail-to-rail input stage structures in literature, we will do a review from their implementation basic ideas

1. For input stages with input transistors working in weak-inversion region, using current complementary circuit to keep the sum of $I_N$ and $I_P$ constant [1][2][6];

2. Using square root circuit to keep $(\sqrt{I_p} + \sqrt{I_n})$ constant [3][13][16];

3. and 4. Using current switches to change the tail current of input differential pairs [3][4][5][6];

5. Using hex-pair structure to control the tail currents of backup pairs [7];
Techniques for N-P Complementary Rail-to-Rail Input Stage (cont’d)

6. Using maximum/minimum selection circuit to conduct the output current of the differential pair with larger current, as well as larger $gm$, to the next stage [8][9];

7. Using electronic zener diode to keep $V_{GSn} + |V_{GSp}|$ constant [10];


We will analyze them one by one in the following sections.

There are still other techniques [12][14][15][17][18], interested readers may check these references.

Note: Unless explicitly stated in this notes, we assume that the square law characteristic of MOS transistors in strong inversion and saturation region. Please notice that for short channel transistors in sub-micron processes, square law is not exactly followed.
Rail-to-Rail Input Stage, Structure 1 [1][2][6]

- For input stages with input transistors working in weak-inversion region, using current complement circuit to keep the sum of $I_N$ and $I_P$ constant.
- Basic idea
  - For CMOS transistors working in weak-inversion region,
    \[
    I_{Dwi} = \frac{W}{L} I_{D0} \exp\left(\frac{V_{GS}}{nKT/q}\right)
    \]
    \[
    g_{mwi} = \frac{W}{L} \frac{I_{D0}}{nKT/q} \exp\left(\frac{V_{GS}}{nKT/q}\right) = \frac{I_{Dwi}}{nKT/q} = k \cdot I_{Dwi}
    \]
    - So, the total transconductance of the input stage is
    \[
    g_{mT} = g_{mN} + g_{mP} = k(I_N + I_P)
    \]
Thus the transconductance of the input stage is proportional to the sum of the tail currents of N and P pairs.

- The following circuit can keep \((I_N + I_P)\) constant.
Rail-to-Rail Input Stage, Structure 1 (cont’d)

- Mb4 and Mb5 mirror the current through Msw, Isw, to provide the tail current of the N-channel input pair. Mb4 and Mb5 are with the same geometry.
- Mb2 always works in saturation region, and never to ohmic region, by properly selecting the gate biasing voltage Vbsw of Msw.
- Msw works as a current switch.
  - When the input common mode voltage, Vicm, is close to Vdd, the P input pair cuts off, the drain current of Mb2, $I_{\text{total}}$ is diverted to Msw. And then mirrored through Mb4 and Mb5, to the source node of the N input pair.
  - When Vicm is close to -Vss, the switch Msw cuts off, $I_{\text{total}}$ then flows to the P input pair.
  - In between, part of $I_{\text{tail}}$ flows to P pair, and the rest to Msw, through current mirror Mb4 and Mb5, to the N pair.
- Using a first order approximation, the following equation stands,
  $$I_p + I_n = I_{\text{tail}} = \text{const}$$
Rail-to-Rail Input Stage, Structure 1 (cont'd)

- The complete circuit
Rail-to-Rail Input Stage, Structure 1 (cont'd)

- Transconductance vs. input common mode voltage

(a) Input transistors working in weak inversion region
(b) Input transistors working in strong inversion region
**Rail-to-Rail Input Stage, Structure 1 (cont’d)**

- **Discussion**
  - This circuit is based on *bipolar* rail-to-rail input stage [1].
  - It has a rail-to-rail constant transconductance only when the input pairs work in *weak inversion* region [2].
  - If the input pairs are in *strong inversion* region, the transconductance will change by a factor of \( 1.4 \ (\sqrt{2}) \).
  - The *area is large*, which is necessary to make the input transistors work in weak inversion region.
  - As working in weak inversion region is a requirement to get a rail-to-rail constant transconductance, this structure only applies to amplifiers with *low GBW*. 
Rail-to-Rail Input Stage, Structure 2
[3][13*][16]

- Using square root circuit to keep \((\sqrt{I_p} + \sqrt{I_n})\) constant
- Basic idea
  - For an input differential pair, using a 1st order approximation,
    \[ gm = \sqrt{2K_p(W/L)}I_D = \sqrt{K_p(W/L)I_{TAIL}} \]
    Where the \(I_{TAIL}\) is the tail current of the differential pair. We can change \(gm\) by altering the tail current of the differential pair!
  - The total transconductance of the input stage is given by
    \[ gm_T = gm_N + gm_P = \sqrt{K_P(W/L)_N}I_N + \sqrt{K_P(W/L)_P}I_P \]
    If \(K_P(W/L)_N = K_P(W/L)_P = 2K\)
    We can get
    \[ gm_T = gm_N + gm_P = \sqrt{2K(\sqrt{I_N} + \sqrt{I_P})} \]
    - To keep \(gm_T\) contant, we just need to keep \((\sqrt{I_N} + \sqrt{I_P})\) contant!

*: [13] is an improved version of this scheme, in [13] \(K_P(W/L)_N = K_P(W/L)_P\) is not required. The authors presented techniques to compensate KP variations.
Rail-to-Rail Input Stage, Structure 2 (cont’d)

- Block diagram

We can utilize the square law characteristic of MOS transistors to implement the square root biasing circuit.
Rail-to-Rail Input Stage, Structure 2 (cont’d)

- The following is one implementation of the rail-to-rail input stage with square root biasing circuit [3].

N-P complementary input stage with square-root circuit
Rail-to-Rail Input Stage, Structure 2 (cont’d)

- Simplified Circuit
Rail-to-Rail Input Stage, Structure 2 (cont’d)

• Analysis

1. \( V_{SG,M123} + V_{SG,M125} = V_{SG,M121} + V_{SG,M124} = \text{const} \),

\[
V_{SG} = \sqrt{\frac{2I_D}{K_P(W/L)}} + |V_{TP}|, \quad \text{as } (W/L)_{M125} = (W/L)_{M123} = (W/L)_{M125,123},
\]

so

\[
\sqrt{\frac{2I_{D,M123}}{K_P(W/L)_{M123,125}}} + |V_{TP}| + \sqrt{\frac{2I_{D,M125}}{K_P(W/L)_{M123,125}}} + |V_{TP}| = \text{const}, \quad \text{that}
\]

is \( \sqrt{I_{D,M123}} + \sqrt{I_{D,M125}} = \text{const}_2 \)

2. \( I_N + I_{SW} = I_{b7} = I_b, \quad I_{D,M122} + I_{SW} = I_{b1} = I_b, \quad \text{and} \quad I_{D,M122} = I_{D,M125} \rightarrow I_N = I_{D,M125} \)

3. \( I_{D,M123} + I_{D,M126} = I_{b6} = I_b, \quad I_{D,M126} + I_P = I_{b2} = I_b, \rightarrow I_P = I_{D,M123} \)

4. From 1. to 3., we can obtain \( \sqrt{I_N} + \sqrt{I_P} = \text{const}_2 \)

5. If M121~M124 are with the same geometry, further calculation yields

\[
\sqrt{I_N} + \sqrt{I_P} = 2\sqrt{I_{D,M121,124}} = 2\sqrt{I_{\text{ref}}}
\]
Rail-to-Rail Input Stage, Structure 2 (cont’d)

• Working Principle
  – The input transistors work in strong inversion region.
  – The square-root circuit M121-M125 keeps the sum of the square-roots of the tail currents of the input pairs and then the gm constant.
  – The current switch, M111, compares the common-mode input voltage with Vb3 and decides which part of the current Ib7 should be diverted to the square-root circuit.
  – In the common-mode input voltage range from Vdd to -Vss+1.8V only the N channel pair operates. The current switch M111 is off and thus the tail current of the N channel input pair $I_N$ equals $I_{b7}=4I_{ref}=20uA$.
  – The sum of the gate-source voltages of M123 and M125 is equal to reference voltage which is realized by M121 and M124. Since the current through M125 equals $I_N$ and the current through M123 equals the tail current of the P channel input pair $I_P$. 

Rail-to-Rail Input Stage, Structure 2 (cont’d)

– It can be calculated that the square-root of $I_p$ is given by

$$
\sqrt{I_p} = 2\sqrt{I_{ref}} - \sqrt{I_N}
$$

Where it is assumed that M121 to M125 are matched.

– In the common-mode input range from $-V_{ss} + 1.2V$ to $V_{ss}$ only the P channel input pair operates. In this range the current $I_{b7} = 4I_{ref} = 20uA$ flows through the current switch to the square-root circuit. Thus, the current through M125 is nearly zero which means that its gate-source voltage is smaller than its threshold voltage.

– If the current through M123 is larger than $4I_{ref} = 20uA$, the current limiter M126 limits the current of M123 to $4I_{ref} = 20uA$ and directs it to the P channel input pair.

– It can be calculated that the transconductance of the input stage, and therefore the unity-gain frequency, is constant within the rail-to-rail input common mode range. The $gm$ is defined by

$$
gm = 2\sqrt{2KI_{ref}} \quad \text{where} \quad K = \frac{1}{2} K_P N \left( \frac{W}{L} \right)_N = \frac{1}{2} K_P P \left( \frac{W}{L} \right)_P
$$
Rail-to-Rail Input Stage, Structure 2 (cont’d)

- The summing circuit M21-M24 adds the output signals of the complementary input stage, and forms the output voltage at node #20.

• Discussion
  - The circuit is somewhat complex and the functionality relies on the square law of MOS transistors. For current sub-micron processes, the square law is not closely followed, which may introduce large error for the total transconductance.
Rail-to-Rail Op Amp Design

Let us design a rail-to-rail input Op Amp with the following specifications utilizing rail-to-rail input stage Structure 2.

<table>
<thead>
<tr>
<th>Specification</th>
<th>Requirement</th>
</tr>
</thead>
<tbody>
<tr>
<td>Process</td>
<td>MOSIS AMI 1.2u</td>
</tr>
<tr>
<td>Power Supply (V\text{sup})</td>
<td>±1.65V</td>
</tr>
<tr>
<td>Load Resistance (R_L)</td>
<td>20 K\Omega</td>
</tr>
<tr>
<td>Load Capacitance (C_L)</td>
<td>20pF</td>
</tr>
<tr>
<td>Power Dissipation (P_D)</td>
<td>&lt;1mW</td>
</tr>
<tr>
<td>DC Gain (A_{v0})</td>
<td>≥80dB</td>
</tr>
<tr>
<td>Gain Bandwidth Product (GBW)</td>
<td>≥1MHz</td>
</tr>
<tr>
<td>Phase Margin (PM)</td>
<td>≥50°</td>
</tr>
<tr>
<td>Slew Rate (SR)</td>
<td>≥2V/\mu S</td>
</tr>
<tr>
<td>Input Common Mode Range (CMR)</td>
<td>rail-to-rail</td>
</tr>
<tr>
<td>Output Voltage Range</td>
<td>-1.45 ~ 1.45 V</td>
</tr>
<tr>
<td>Output Stage</td>
<td>Simple Class A</td>
</tr>
</tbody>
</table>
Rail-to-Rail Op Amp Design (cont’d)

- The block diagram of the 2-stage operational amplifier is shown in the following

- We add $R_z$ in this diagram compared with the figure in slide #8, which is used to cancel the zero generated by $C_m$. When $R_z = 1/gm_2$, the zero is cancelled.
When $R_z = 1/gm^2$, the transfer characteristics of the amplifier is given by

$$A(s) \approx \frac{g_{m1}g_{m2}}{s^2C_LC_m + sC_mg_{m2} + g_{o1}g_L} = \frac{A_0}{s^2 \frac{1}{p_1p_2} + s \frac{1}{p_1} + 1}$$

where $A_0 = \frac{g_{m1}g_{m2}}{g_{o1}g_L}$, $p_1 = \frac{GBW}{A_0} = \frac{g_{m1}}{C_m}A_0$, $p_2 = \frac{g_{m2}}{C_L}$,

and $GBW = \frac{g_{m1}}{C_m}$.

The rail-to-rail input stage of the amplifier is shown on slide #25.
Rail-to-Rail Op Amp Design (cont’d)

- The second stage, or output stage, of the amplifier (M220 and Mb6) is a simple inverter with Miller frequency compensation (Cm and M221).

M221 is a MOSFET which works in linear region, taking the role of Rz.
Mb6 works as a current source.
Rail-to-Rail Op Amp Design (cont’d)

- Design procedure

1) Tail current and input transistors

\[ GBW (rad/s) = \frac{g_{m1}}{C_m} \]

Let \( C_m = \frac{1}{2} C_L \), then we can get

\[ g_{m1} = GBW \times C_m = 2\pi \times 1MHz \times 10\ pF = 62.8\mu A/V \]

To leave some margin for the GBW, let \( g_{m1} = 80\mu A/V \).

\[ SR = \frac{I_{TAIL}}{C_m}, \ so \]

\[ I_{TAIL} = SR \times C_m = 2V / \mu S \times 10\ pF = 20\mu A \]

let \( I_{TAIL} = 25\mu A \).

For P pair

\[ (W/L)_{P-PAIR} = \frac{g_{m1}^2}{2K_{pp}I_D} = \frac{g_{m1}^2}{K_{pp}I_{TAIL}} = \frac{(80\mu A/V)^2}{19346 \times 10^{-5} A/V^2 \times 25\mu A} = 13.23 \]

To make layout convenient, we choose \( (W/L)_{P-PAIR} = 16 \).
Rail-to-Rail Op Amp Design (cont’d)

To make layout convenient, we choose \((W/L)_{p-pair} = 16\).

To make N pair and P pair be symmetrical, we should let

\[
K_{pN} \left( \frac{W}{L} \right)_{N-pair} = K_{pP} \left( \frac{W}{L} \right)_{P-pair}, \text{ so}
\]

\[
\left( \frac{W}{L} \right)_{N-pair} = \left( \frac{W}{L} \right)_{P-pair} \frac{K_{pP}}{K_{pN}} = 16 \times \frac{1.9346 \times 10^{-5} \ A/V^2}{7.3584 \times 10^{-5} \ A/V^2} = 4.207, \text{ choose}
\]

\[
\left( \frac{W}{L} \right)_{N-pair} = 4.
\]

For current sources \(I_{b1}, I_{b2}, I_{b3}, I_{b4}, I_{b6}, \) and \(I_{b7}\) are all with the same value \(I_{TAIL}=25\mu A. \)

\(I_{ref}\) is \(I_{TAIL}/4=6.25\mu A.\)

2) **Current switch M\(_{111}\)**

M\(_{111}\) works in saturation region when it is on and cut off region when it is off as the common mode voltage swings from rail-to-rail.

The \(V_{GS}\) of switch transistor controls the current transition region width with the common mode voltage. There are some disadvantages if the transition region is too narrow. We choose \(V_{dsat,M_{111}}=0.5\)V when all of the current \(I_{b7}\) flows through \(M_{111}\).
Rail-to-Rail Op Amp Design (cont’d)

\[
\left( \frac{W}{L} \right)_{M111} = \frac{2I_D}{K_{PN} V_{dsat, M111}^2} = \frac{2 \times 25 \mu A}{7.3584 \times 10^{-5} A/V^2 \times (0.5V)^2} = 2.718, \\
\]

Let \( \left( \frac{W}{L} \right)_{M111} = 3 \).

3) Square root circuit, \( M_{121} - M_{126} \)

We should select a proper working point for this part of circuit to obtain a good square root characteristic. If the overdrive voltage \( V_{ov} = V_{dsat} = (V_{GS} - V_T) \) is too low, the MOSFET may work near the transition region, which is between strong inversion and weak inversion region.

If \( V_{ov} \) is too large, because of velocity saturation effect, the \( I_{DS} \) vs. \( V_{DS} \) characteristic may become somewhat near linear rather than quadratic, which will also introduce some error.

Let us select \( V_{ov} = 0.3V \),

\[
\left( \frac{W}{L} \right)_{M121 - M125} = \frac{2I_D}{K_{pp} V_{dsat}^2} = \frac{2 \times 25 \mu A}{1.9346 \times 10^{-5} A/V^2 \times (0.3V)^2} = 28.72, \\
\]
Rail-to-Rail Op Amp Design (cont’d)

Choose \( \frac{W}{L}_{M_{121} - M_{125}} = 28 \).

\( M_{126} \) is just a level shift transistor, its size is not critical, we just let \( \frac{W}{L}_{M_{126}} = 28 \).

4) Summing circuit, \( M_{21} \sim M_{24}, M_{211}, \) and \( M_{212} \)

\( M_3, M_{21} \) and bias current \( I_{b2} \) form folded cascode structure, as well as \( M_4, M_{22} \) and bias current \( I_{b3} \). Although the quiescent current through \( M_{21} (M_{22}) \) is \( I_{TAIL}/2 \), its maximum current is \( I_{TAIL} \).

Let \( V_{dsat} \) of \( M_{21} (M_{22}) \) to be 0.25V when it is conducting \( I_{TAIL} \), we can get

\[
\left( \frac{W}{L} \right)_{M_{21},M_{22}} = \frac{2I_D}{K_{pp}V_{dsat}^2} = \frac{2 \times 25 \mu A}{1.9346 \times 10^{-5} A/V^2 \times (0.25V)^2} = 41.3522 ,
\]

Choose \( \left( \frac{W}{L} \right)_{M_{21},M_{22}} = 40 \).

Similarly for \( M_{23} (M_{24}) \), we get \( \left( \frac{W}{L} \right)_{M_{23},M_{24}} = 12 \).
40

Rail-to-Rail Op Amp Design (cont’d)

The maximum drain current for \( M_{211} \) and \( M_{212} \) is \( 2I_{TAIL} \). We can get

\[
\frac{W}{L}_{M_{211},M_{212}} = 24.
\]

5) The output stage \( M_{220} \) and \( M_{221} \)

To have an output swing from rail-to-rail, the minimum biasing current should be

\[
I_{D,BIAS,min} = I_{RL,max} = \frac{Vdd}{R_L} = \frac{1.65V}{20K\Omega} = 82.5\mu A
\]

To leave some margin, we choose the bias current as 100\( \mu \)A.

To have a rail-to-rail swing from \( V_{dd}-0.2V \) to \( -V_{ss}+0.2V \) as required by the design specification, we should have a small \( V_{dsat} \) for the \( M_{220} \), we choose \( V_{dsat,M220}=0.2V \), the geometry ratio of \( M_{220} \) is given by

\[
\frac{W}{L}_{M_{220}} = \frac{2I_D}{K_{PN}V_{dsat}} = \frac{2 \times 100\mu A}{7.3584 \times 10^{-5} A/V^2 \times (0.2V)^2} = 67.95,
\]

We choose \( \frac{W}{L}_{M_{220}} = 68 \).
Rail-to-Rail Op Amp Design (cont’d)

Let us check whether $g_{m2}$ can satisfy the phase margin requirement or not. There should be $p_2 = \frac{g_{m2}}{C_L} \geq 2.5GBW$.

Let us calculate $g_{m2}$ first,

$$g_{m2} = \sqrt{2I_D K_{PN} \left( \frac{W}{L} \right)_{M220}} = \sqrt{2 \times 100 \mu A \times 7.3584 \times 10^{-5} \frac{A}{V^2} \times 68} = 1000.3 \mu A/V$$

So

$$p_2 = \frac{g_{m2}}{C_L} = \frac{1000.3 \mu A/V}{20 \text{ pF}} = 50.02 \times 10^6 \text{ rad} / \text{s} = 7.96 \text{ MHz} \geq 2.5 \text{ GBW} = 2.5 \text{ MHz},$$

the phase margin specification can be satisfied.

Actually, if we ignore other higher non-dominant poles except $p_2$, we can calculate the phase margin as

$$PM = 180^\circ - \tan^{-1} \frac{GBW}{p_1} - \tan^{-1} \frac{GBW}{p_2}$$

$$\approx 90^\circ - \tan^{-1} \frac{g_{m1}}{C_m} = 90^\circ - \tan^{-1} \frac{80 \mu A/V}{10 \text{ pF}} = 80.9^\circ$$

$$\approx 90^\circ - \tan^{-1} \frac{g_{m2}}{C_L} = \frac{80 \mu A/V}{10 \text{ pF}} \times 50.02 \times 10^6 \text{ rad} / \text{s} = 80.9^\circ$$
Rail-to-Rail Op Amp Design (cont’d)

For $M_{221}$, which works in diode region and with bulk connected to $-V_{ss}$, we can get its $V_T$ as,

$$V_{T,M_{221}} = V_{TO} + \gamma (\sqrt{2|\phi_F| - V_{BS,M_{221}}} - \sqrt{2|\phi_F|})$$

$$= V_{TO} + \gamma (\sqrt{2|\phi_F| + V_{GS,M_{220}}} - \sqrt{2|\phi_F|})$$

$$= 0.6443V + 0.7003V^{1/2} (\sqrt{0.7V + (0.2 + 0.6443)V} - \sqrt{0.7V}) = 0.9286V$$

$$\left(\frac{W}{L}\right)_{M_{221}} = \frac{g_m}{K_{PN} (V_{sup} - V_{T,M_{221}} - V_{GS,M_{220}})} = 8.903 ,$$

Choose $\left(\frac{W}{L}\right)_{M_{221}} = 9$.

6) Bias voltages $V_{b1}$, $V_{b3}$ and $V_{b4}$

a) $V_{b1}$

Assume voltage drop for $I_{b1}$ is 0.4V,

$$|V_{GS,M_{122}}| = \sqrt{\frac{2I_D}{K_{PP} (W/L)_{M_{122}}}} + |V_{T,M_{122}}| = 1.209V$$
Rail-to-Rail Op Amp Design (cont’d)

Thus

\[ V_{b1} = V_{\text{drop,}Ib1} + |V_{GS,M122}| = 1.61V, \text{ let } V_{b1} = 1.6V \]

a) \( V_{b2}, V_{b3} \) and \( V_{b4} \)

Similarly, we can calculate \( V_{b2} \) as

\[ V_{b2} = V_{\text{drop,}Ib7} + V_{GS,M111} = 1.67V, \text{ let } V_{b2} = 1.7V. \]

For \( V_{b3} \) and \( V_{b4} \),

\[ V_{b3} = V_{\text{drop,M211}} + V_{GS,M23} = 1.44V, \text{ let } V_{b3} = 1.5V. \]
\[ V_{b4} = V_{\text{drop,}Ib2} + |V_{GS,M21}| = 1.55V, \text{ let } V_{b4} = 1.6V. \]

7) Modifications according to HSPICE simulation

HSPICE simulation shows that all specifications are met without any changes to the parameters calculated above, but the output voltage swing, only from –1.6V to 1.4V. Change the bias current of the output stage from 100\( \mu \)A to 125\( \mu \)A. The total power consumption increase by about 80\( \mu \)W to 0.938mW, but still meets the specification.
Rail-to-Rail Op Amp Simulation Results

- Simulation results
  - DC input/output characteristics

![Graph showing DC gain of 4.51×10⁴](image)

DC Gain = 4.51×10⁴
Rail-to-Rail Op Amp Simulation Results (cont’d)

- Frequency response

![Graph showing frequency response with key points labeled: GBW=1.082 MHz, $A_v_0=93.25$ dB, Phase Margin = 80.7°.](image-url)
Rail-to-Rail Op Amp Simulation Results (cont’d)

- Transient response (as a unity gain buffer, output voltage swing -1.5V ~ 1.5V)

![Graph showing input voltage, output voltage, and time (sec)]

- $SR_+ = 2.2 \text{ V/}\mu\text{S}$
- $SR_- = 2.3 \text{ V/}\mu\text{S}$

- Output Voltage
- Input Voltage
Rail-to-Rail Op Amp Simulation Results (cont’d)

- Tail currents vs. common mode voltage

Note: The switching point can be set by $V_{b2}$ in the diagram on slide #25. The transition slope can be controlled by the (W/L) of M11.
Rail-to-Rail Op Amp Simulation Results (cont’d)

- First stage transconductance vs. common mode voltage

<table>
<thead>
<tr>
<th>Gm TOTAL (µA/V)</th>
<th>Average</th>
<th>Minimum</th>
<th>Maximum</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>77.5</td>
<td>68.1</td>
<td>82.3</td>
</tr>
</tbody>
</table>

Deviation

-12.3% 6.2%
Rail-to-Rail Op Amp Simulation File

- HSPICE file

2-Stage Op Amp with Rail-to-Rail Input Structure 2

```
.options list node post
.include ami_n8cu_level3
.op

* Parameter definitions

.param lam = 0.6u ln = 2.4u lp=2.4u ln3=4.8u lp1=4.8u
+ wp1=76.8u wn3=19.2u wn111=7.2u wp121=67.2u wp21=96u
+ wn23=28.8u wn211=57.6u
+ wpb1=153.6u wnb7=48u wnb8=12u
+ wn220=163.2u wn221=21.6u

* Netlist

m1 10 ninm 2 2 cmosp W=wp1 L=lp1 AD='5*lam*wp1' AS='5*lam*wp1'
+ PS='2*wp1+10*lam' PD='2*wp1+10*lam'
m2 11 ninp 2 2 cmosp W=wp1 L=lp1 AD='5*lam*wp1' AS='5*lam*wp1'
+ PS='2*wp1+10*lam' PD='2*wp1+10*lam'
m3 8 ninm 1 nvss cmosn W=wn3 L=ln3 AD='5*lam*wn3' AS='5*lam*wn3'
+ PS='2*wn3+10*lam' PD='2*wn3+10*lam'
m4 9 ninp 1 nvss cmosn W=wn3 L=ln3 AD='5*lam*wn3' AS='5*lam*wn3'
+ PS='2*wn3+10*lam' PD='2*wn3+10*lam'
m111 5 nvb2 1 nvss cmosn W=wn111 L=ln AD='5*lam*wn111' AS='5*lam*wn111'
+ PS='2*wn111+10*lam' PD='2*wn111+10*lam'
```
Rail-to-Rail Op Amp Simulation File (cont’d)

m121 7 7 nvdd nvdd cmosp W=wp121 L=lp AD='5*lam*wp121' AS='5*lam*wp121'
  + PS='2*wp121+10*lam' PD='2*wp121+10*lam'
m122 4 n vb4 5 nvdd cmosp W=wp121 L=lp AD='5*lam*wp121' AS='5*lam*wp121'
  + PS='2*wp121+10*lam' PD='2*wp121+10*lam'
m123 3 4 nvdd nvdd cmosp W=wp121 L=lp AD='5*lam*wp121' AS='5*lam*wp121'
  + PS='2*wp121+10*lam' PD='2*wp121+10*lam'
m124 6 6 7 7 cmosp W=wp121 L=lp AD='5*lam*wp121' AS='5*lam*wp121'
  + PS='2*wp121+10*lam' PD='2*wp121+10*lam'
m125 nvss 6 4 4 cmosp W=wp121 L=lp AD='5*lam*wp121' AS='5*lam*wp121'
  + PS='2*wp121+10*lam' PD='2*wp121+10*lam'
m126 3 3 2 2 cmosp W=wp121 L=lp AD='5*lam*wp121' AS='5*lam*wp121'
  + PS='2*wp121+10*lam' PD='2*wp121+10*lam'

m21 12 n vb1 8 nvdd cmosp W=wp21 L=lp AD='5*lam*wp21' AS='5*lam*wp21'
  + PS='2*wp21+10*lam' PD='2*wp21+10*lam'
m22 20 n vb1 9 nvdd cmosp W=wp21 L=lp AD='5*lam*wp21' AS='5*lam*wp21'
  + PS='2*wp21+10*lam' PD='2*wp21+10*lam'
m23 12 n vb3 10 nvss cmosp W=wn23 L=ln AD='5*lam*wn23' AS='5*lam*wn23'
  + PS='2*wn23+10*lam' PD='2*wn23+10*lam'
m24 20 n vb3 11 nvss cmosp W=wn23 L=ln AD='5*lam*wn23' AS='5*lam*wn23'
  + PS='2*wn23+10*lam' PD='2*wn23+10*lam'

m211 10 12 nvss nvss cmosp W=wn211 L=ln AD='5*lam*wn211' AS='5*lam*wn211'
  + PS='2*wn211+10*lam' PD='2*wn211+10*lam'
m212 11 12 nvss nvss cmosp W=wn211 L=ln AD='5*lam*wn211' AS='5*lam*wn211'
  + PS='2*wn211+10*lam' PD='2*wn211+10*lam'
m220 nout 20 nvss nvss cmosp W=wn220 L=ln AD='5*lam*wn220' AS='5*lam*wn220'
  + PS='2*wn220+10*lam' PD='2*wn220+10*lam'
Rail-to-Rail Op Amp Simulation File (cont’d)

m221 20 nvdd 21 nvss cmosn W=wn221 L=ln AD='5*lam*wn221' AS='5*lam*wn221' + PS='2*wn221+10*lam' PD='2*wn221+10*lam'

mb1 30 30 nvdd nvdd cmosp W=wpb1 L=lp AD='5*lam*wpb1' AS='5*lam*wpb1' + PS='2*wpb1+10*lam' PD='2*wpb1+10*lam'
mb2 5 30 nvdd nvdd cmosp W=wpb1 L=lp AD='5*lam*wpb1' AS='5*lam*wpb1' + PS='2*wpb1+10*lam' PD='2*wpb1+10*lam'
mb3 2 30 nvdd nvdd cmosp W=wpb1 L=lp AD='5*lam*wpb1' AS='5*lam*wpb1' + PS='2*wpb1+10*lam' PD='2*wpb1+10*lam'
mb4 8 30 nvdd nvdd cmosp W=wpb1 L=lp AD='5*lam*wpb1' AS='5*lam*wpb1' + PS='2*wpb1+10*lam' PD='2*wpb1+10*lam'
mb5 9 30 nvdd nvdd cmosp W=wpb1 L=lp AD='5*lam*wpb1' AS='5*lam*wpb1' + PS='2*wpb1+10*lam' PD='2*wpb1+10*lam'
mb6 nout 30 nvdd nvdd cmosp W=wpb1 L=lp AD='5*lam*wpb1' AS='5*lam*wpb1' + PS='2*wpb1+10*lam' PD='2*wpb1+10*lam' M=5

mb7 40 40 nvss nvss cmosn W=wnb7 L=ln AD='5*lam*wnb7' AS='5*lam*wnb7' + PS='2*wnb7+10*lam' PD='2*wnb7+10*lam'
mb8 6 40 nvss nvss cmosn W=wnb8 L=ln AD='5*lam*wnb8' AS='5*lam*wnb8' + PS='2*wnb8+10*lam' PD='2*wnb8+10*lam'
mb9 3 40 nvss nvss cmosn W=wnb7 L=ln AD='5*lam*wnb7' AS='5*lam*wnb7' + PS='2*wnb7+10*lam' PD='2*wnb7+10*lam'
mb10 1 40 nvss nvss cmosn W=wnb7 L=ln AD='5*lam*wnb7' AS='5*lam*wnb7' + PS='2*wnb7+10*lam' PD='2*wnb7+10*lam'

cm nout 21 10p
Rail-to-Rail Op Amp Simulation File (cont’d)

* Load
  cl nout 0 20p
  rl nout 0 20k

* Current & voltage sources
  irefp 30 nvss 25u
  irefn nvdd 40 25u
  vb1 nvdd nvb1 1.6
  vb4 nvdd nvb4 1.6
  vb2 nvb2 nvss 1.7
  vb3 nvb3 nvss 1.5
  einp ninp ncm input 0 0.5
  einm ninm ncm input 0 -0.5
  vcm ncm 0 0
  vin input 0 -3.824e-5 ac = 1
  vdd nvdd 0 1.65
  vss nvss 0 -1.65

* Test cards
  .dc vin -0.5m 0.5m 10u
  .ac dec 100 2 100x
  .probe ac vdb(nout)

.end
Rail-to-Rail Input Stage, Structure 3 [3][4][6]

- Using current switches to change the tail current of input differential pairs

- Basic idea
  - We know that, by first order approximation, for a MOS transistor working in strong inversion and saturation region, square law applies, that is

\[ I_D = K(V_{GS} - V_T)^2, \text{ and } \quad gm = 2\sqrt{KI_D}, \]

where

\[ K = \frac{1}{2} KP\left(\frac{W}{L}\right) \]

- Suppose for the N and P input pairs, \( KP_N\left(\frac{W}{L}\right)_N = KP_P\left(\frac{W}{L}\right)_P = 2K \)

and the tail currents of N and P pairs are equal, with the value of \( I_{\text{tail}} \).
Rail-to-Rail Input Stage, Structure 3 (cont’d)

– When the input common mode voltage is in the mid-range, both of N and P pairs are conducting, so the total transconductance is

\[ g_{m_T} = g_{m_N} + g_{m_P} = 2\sqrt{2K_{TAIL}} \]

– When the input common mode voltage is close to Vdd, the N pair operates. And when it is close to the -Vss, the P pair operates. In both cases, the total transconductance is only half of that when both of N and P pairs operate.

\[ g_{m_T} = g_{m_N} = g_{m_P} = \sqrt{2K_{TAIL}} \]

We can increase the tail current to 4 times of its original value to have the same transconductance as that when both of N and P pairs operate.
Rail-to-Rail Input Stage, Structure 3 (cont’d)

- The circuit
Rail-to-Rail Input Stage, Structure 3 (cont’d)

- Conceptual circuit

- When common mode input voltage, Vicm, is close to \(-V_{ss}\), SW1B and SW2A are on, and SW1A and SW2B off.
- When Vicm is close to Vdd, SW1A and SW2B are on, and SW1B and SW2A off.
- In between, SW1B and SW2B are on, SW1A and SW2A off.
- In practice, SW1B and SW2B are never required, just short circuits. Say, if SW1A is on, Ibp will be diverted to the 1:3 current mirror; if SW1A is off, Ibp will provide tail current for M1 and M2.
Rail-to-Rail Input Stage, Structure 3 (cont’d)

- Working principle
  - If both of the input pairs operate, the total gm of the complementary input stage is 2 times of the gm with one single pair. In order to obtain the same gm when only one of the pairs operates, the tail current has to be 4 times larger.
  - The current switches M116 and M124 compare the common mode input voltage with with Vb2=1.4V and Vb4=1.4V, respectively. In the common mode input range from Vss to Vss+1.3V only the P channel input pair operates. In this range, the current switch M116 conducts while M124 is off. The current Iref1=5uA now flows through M116 to a 1:3 current multiplier M121-M122. Since Iref1 is equal to Iref2, I_p equals 4Iref1=20uA.
  - In the common mode input range from Vss+1.5V to Vdd-1.5V both of the input pairs operate. In this range, M116 and M124 are off, and the tail currents of N and P pairs are 5uA.
Rail-to-Rail Input Stage, Structure 3 (cont’d)

- In the common mode input range from Vdd-1.3V to Vdd, only the N channel pair operates. The current switch M124 conducts while M116 is off. The current Iref2=5uA now flows through M124 to a 1:3 current multiplier M113-M114. \(I_N\) equals 4Iref2=20uA.

- It can be calculated that for each input range, the total gm is

\[
gm = 2\sqrt{2KI\text{ref}}\quad \text{where} \quad K = \frac{1}{2} KP_N \left(\frac{W}{L}\right)_N = \frac{1}{2} KP_P \left(\frac{W}{L}\right)_P
\]

- In the takeover regions of the current switches, Vss+1.3V to Vss+1.5V and Vdd-1.5V to Vdd-1.3V, the total gm of the input stage increases with about 15% above its nominal value.

Which can be proved by the following analysis.

If the common mode input voltage is between Vss+1.3V and Vss+1.5V, the M116 is partly conducting, and the rest of tail current flows through M3 and M4, which is assumed to be Ix here. So the tail current of the P pair is Iref+3(Iref-Ix).
The total $gm$ of the input stage is given by

$$gm_T = \sqrt{2K} (\sqrt{I_x} + \sqrt{I_{\text{ref}}} + 3(I_{\text{ref}} - I_x))$$

Calculate the maximum value of this equation, we can obtain that when $I_x = \frac{1}{3}I_{\text{ref}}$, $gm_T$ has its maximum value. Which yields

$$gm_T = \sqrt{2K}I_{\text{ref}} \left(\sqrt{\frac{1}{3}} + \sqrt{3}\right) = 2.31\sqrt{2KI_{\text{ref}}} = 2\sqrt{2KI_{\text{ref}}} (1 + 15.5\%)$$

Which is about 15% larger than its nominal value $2\sqrt{2KI_{\text{ref}}}$. 

Rail-to-Rail Input Stage, Structure 3 (cont’d)

- Transconductance vs. input common mode voltage

![Graph showing transconductance vs. input common mode voltage for rail-to-rail input stages with and without gm control.}

- Rail-to-rail input stage with current switch
- Rail-to-rail input stage without gm control
Rail-to-Rail Input Stage, Structure 4 [5]

• Another constant-gm input stage with current-switch. When only N ( or P ) input pair works, activate another N ( or P ) pair ( we call it backup pair ) to compensate the transconductance loss.

• Basic idea
  – In the previous constant-gm rail-to-rail input stage, when the common mode input voltage is in the middle range, both of the P and N pairs are operating, the total bias current is \( I_N + I_P = 2I_S \) ( \( I_N = I_P = I_S \) ). But when the common mode voltage is close to \( V_{DD} \) or \( -V_{SS} \), only one of the differential pairs operates, the bias current is \( 4I_S \). So the slew rate of the amplifier is the function of the common mode voltage, and has the variation of 2 times.
  – How can we keep the gm constant, and at the same time the slew rate not to vary so much? …
  – We can have 2 N-type pairs and 2 P-type pairs. One N pair ( or P pair ) are biased normally, we call it main pair. But another N pair ( or P pair ), the backup pair, is biased by the current steered from the main P pair ( or N pair ) if the main P pair can not work properly -- the current may also be controlled by current switch.
Rail-to-Rail Input Stage, Structure 4 (cont’d)

- The circuit [4]
Rail-to-Rail Input Stage, Structure 4 (cont’d)

- Working principle

  - When the common mode input voltage is in the middle range, P type pair (M1A, M2A) and N type pair (M3A, M4A) operate. Both of M7 and M10, which work as current switches, are off, thus there is no tail current flowing through the backup pairs (M1B, M2B) and (M3B, M4B). The total transconductance $\text{gm}_T = \text{gm}_P + \text{gm}_N = 2\text{gm}$ (assume $I_{\text{ref}1} = I_{\text{ref}2} = I_{\text{ref}}$, and $K_P N (W/L)_N = K_P P (W/L)_P$). The sum of the tail currents is $I_{\text{ref}1} + I_{\text{ref}2} = 2I_{\text{ref}}$.

  - When the common mode input voltage is close to $V_{DD}$, the current switch M10 is on, and $I_{\text{ref}2}$ is steered through M10, mirrored by current mirror M5 and M6, and provides the tail current with the value of $I_{\text{ref}}$ for the N type differential pair (M3B and M4B). The total transconductance $\text{gm}_T = 2\text{gm}$, the sum of the tail currents is $2I_{\text{ref}}$. 
Rail-to-Rail Input Stage, Structure 4 (cont’d)

– When the common mode input voltage is close to $V_{DD}$, the current switch M7 is on, and $I_{ref1}$ flows through M7, mirrored by current mirror formed with M8 and M9, and provides the tail current with the value of $I_{ref}$ for the P type differential pair (M1B, M2B). The total transconductance $g_{mT}=2g_{m}$, the sum of the tail currents is $2I_{ref}$.

– Actually, the N backup pair (M3B, M4B) takes the role of primary P pair (M1A, M2A) when $V_{icm}$ is close to $V_{DD}$ and the current switch M10 is on. The P backup pair (M1B, M2B) takes the role of primary P pair (M3A, M4A) when $V_{icm}$ is close to $-V_{SS}$ and the current switch M7 is on.
Rail-to-Rail Input Stage, Structure 4 (cont’d)

- Transconductance vs. input common mode voltage

![Graph showing transconductance vs. input common mode voltage]

- With constant gm control
- Without constant gm control
We may notice that there are 2 bumps on the gm curve, where the transconductance is 20% greater than its nominal value. The bumps are at take-over regions.

By simple analysis we can know why it is so. If \( V_{icm} \) is at its upper take-over region (close to \( V_{DD} \)), assume that the tail current of the primary P pair \( I_{PA} \) is \( I_x \), then the tail current of the primary N pair \( I_{NA} \) is \( I_{ref} \), and tail current of the backup N pair \( I_{NB} \) is \( I_{ref} - I_x \). The total transconductance is

\[
G_m = \sqrt{2K} \left( \sqrt{I_{ref}} + \sqrt{I_x} + \sqrt{I_{ref} - I_x} \right)
\]

Calculate the maximum value of this expression, we can get, when \( I_x = I_{ref}/2 \), \( G_m \) has its maximum value, which is

\[
G_m = \sqrt{2KI_{ref}} \left( \sqrt{2} + 1 \right) = 2.4\sqrt{2KI_{ref}}
\]

which is about 20% larger than its nominal value \( 2\sqrt{2KI_{ref}} \).
Rail-to-Rail Op Amp Design

Let us design a rail-to-rail input Op Amp with the same specifications on slide #31 utilizing rail-to-rail input stage Structure 4.

- **Design procedure**

  1) **Tail current and input transistors**

      By the same procedure we have discussed in slide #35, we can get the geometry ratios for N and P input pairs as \((W / L)_{P-PAIR} = 16\) and \((W / L)_{N-PAIR} = 4\).

      For this structure, both of the N pair and P pair are actually divided into 2 branches each. Let us say the N half, one is the main differential pair (\(M_{3A}\) and \(M_{4A}\)), which operates if the common mode voltage is at its working region, the other is backup pair (\(M_{3B}\) and \(M_{4B}\)), which operates only if the P channel main pair (\(M_{1A}\) and \(M_{2A}\)) cannot operate and the input common mode voltage turns on the current switch \(M_{10}\). The current switch \(M_{10}\) and the current mirror (\(M_5\) and \(M_6\)) accomplish the takeover.
The geometry ratios of the input pairs should be divided by 2, so
\[
(W / L)_{P-PAIR}' = \frac{(W / L)_{P-PAIR}}{2} = 8 \quad \text{and} \quad (W / L)_{N-PAIR}' = \frac{(W / L)_{N-PAIR}}{2} = 2.
\]

The tail current \(I_{TAIL}\) (which is 25\(\mu\)A as calculated in the previous design) is also divided into 2 branches, so \(I_{TAIL}' = 12.5\mu\)A = \(I_{ref2}/2 = I_{ref1} \).

2) Current switches, M7 and M10

The \(V_{GS}\) of switch transistors M7 and M10 controls the current transition region width with the common mode voltage. We should avoid overlapping N and P transition regions, because in the transition region, the total \(gm\) deviates from its nominal value. If the 2 transition regions get together, the deviations will also add together. -- Let us say the extreme case that the transition regions overlap exactly, and at one point of the common mode voltage, each of the 4 pairs conducts tail current with the same magnitude, \(I_{TAIL}'/2\). The total \(gm\) will be \(\sqrt{2}\) times of its nominal value at this point, the same with structure 1 working in strong inversion region!
Rail-to-Rail Op Amp Design (cont’d)

So we choose \( V_{\text{dsat, } M7} = V_{\text{dsat, } M10} = 0.25 \text{V} \), a relatively small value to avoid overlapping,

\[
\left( \frac{W}{L} \right)_{M7} = \frac{2I_D}{K_{PN} V_{\text{dsat, } M7}} = \frac{2 \times 12.5 \mu A}{7.3584 \times 10^{-5} \text{A/V}^2 \times (0.25 \text{V})^2} = 5.436 ,
\]

Choose \( \left( \frac{W}{L} \right)_{M7} = 5 \).

\[
\left( \frac{W}{L} \right)_{M10} = \frac{2I_D}{K_{PP} V_{\text{dsat, } M10}} = \frac{2 \times 12.5 \mu A}{1.9346 \times 10^{-5} \text{A/V}^2 \times (0.25 \text{V})^2} = 20.67 ,
\]

Choose \( \left( \frac{W}{L} \right)_{M10} = 20 \).

To avoid overlapping the 2 transition regions, in addition to have a small \( V_{\text{GS}} \) for \( M_7 \) and \( M_{10} \), we should also carefully select the takeover voltages \( V_{b1} \) and \( V_{b2} \). That is, \( V_{b1} \) and \( V_{b2} \) should be small enough to separate the two transitions regions apart, so the takeover voltage for \( M_7 \) is close to \( -V_{\text{ss}} \), and that of \( M_{10} \) close to \( V_{\text{dd}} \).
Rail-to-Rail Op Amp Design (cont’d)

Let us assume when $M_7$ is fully on, the minimum voltage at source of $M_7$ is $-V_{ss}+0.25V$, the $0.25V$ is for the $V_{DS}$ of the current source $I_{ref1}$. Then

$$V_{T,M_7} = V_{TO} + \gamma \left( \sqrt{2 |\phi_F|} - V_{BS,M_7} - \sqrt{2 |\phi_F|} \right)$$

$$= 0.6443V + 0.7003V^{1/2} (\sqrt{0.7V} + 0.25V - \sqrt{0.7V}) = 0.7410V,$$

$$V_{b2} = V_{dsat, Iref1} + V_{T,M_7} + V_{dsat,M_7} = 0.25V + 0.7410V + \sqrt{\frac{2I_{TAIL}}{(W/L)_{M7} nKP}} = 1.251V,$$

to leave some margin, let $V_{b2}=1.3V$,

Similarly, we can get the bias voltage source $V_{b1}$ as $1.33V$, let $V_{b1}=1.35V$.

3) Summing circuit, $M_{21}$~$M_{24}$, $M_{211}$, and $M_{212}$, and output stage $M_{220}$ and $M_{221}$

These 2 parts are the same with the design procedure on slide #38 and #39.

4) Modifications according to HSPICE simulation

No modifications for the input stage. For the output stage we just increased the bias current to $125\mu A$ to increase the output voltage swing.
Rail-to-Rail Op Amp Simulation Results

- Simulation results (as DC input output characteristics, and frequency response are very similar with those of previous design, we do not plot here).
  - Transient response

![Graph showing transient response with labels SR+ = 2.2 V/µS and SR- = 2.3 V/µS]
Rail-to-Rail Op Amp Simulation Results (cont’d)

- Tail currents v.s. common mode voltage

![Graph showing tail currents vs. common mode voltage]
Rail-to-Rail Op Amp Simulation Results (cont’d)

- Transconductance v.s. common mode voltage

<table>
<thead>
<tr>
<th></th>
<th>Average</th>
<th>Minimum</th>
<th>Maximum</th>
</tr>
</thead>
<tbody>
<tr>
<td>$G_{m_{TOTAL}}$ (uA/V)</td>
<td>83.2</td>
<td>78.1</td>
<td>95</td>
</tr>
<tr>
<td>Deviation</td>
<td>-6.2%</td>
<td>14.2%</td>
<td></td>
</tr>
</tbody>
</table>
Rail-to-Rail Op Amp Simulation File

- HSPICE file

2-Stage Op Amp with Rail-to-Rail Input Structure 4

```plaintext
.options list node post
.include ami_n8cu_level3
.op

* Parameter definitions

.param lam = 0.6u ln = 2.4u lp=2.4u ln3=3.6u lp1=3.6u
  + wp1=28.8u wn3=7.2u wn5=21.6u wp8=28.8u wn7=12u wp10=48u
  + wp21=96u wn23=28.8u wn26=57.6u wpb1=76.8u wnb10=24u
  + wn220=163.2u wn221=21.6u

* Netlist

m1a 10 ninm 2 2 cmosp W=wp1 L=lp1 AD='5*lam*wp1' AS='5*lam*wp1'
  + PS='2*wp1+10*lam' PD='2*wp1+10*lam'
m2a 11 ninp 2 2 cmosp W=wp1 L=lp1 AD='5*lam*wp1' AS='5*lam*wp1'
  + PS='2*wp1+10*lam' PD='2*wp1+10*lam'
m1b 10 ninm 4 4 cmosp W=wp1 L=lp1 AD='5*lam*wp1' AS='5*lam*wp1'
  + PS='2*wp1+10*lam' PD='2*wp1+10*lam'
m2b 11 ninp 4 4 cmosp W=wp1 L=lp1 AD='5*lam*wp1' AS='5*lam*wp1'
  + PS='2*wp1+10*lam' PD='2*wp1+10*lam'
```
Rail-to-Rail Op Amp Simulation File (cont’d)

m3a 8 ninm 1 nvss cmosn W=wn3 L=ln3 AD='5*lam*wn3' AS='5*lam*wn3'
+ PS='2*wn3+10*lam' PD='2*wn3+10*lam'
m4a 9 ninp 1 nvss cmosn W=wn3 L=ln3 AD='5*lam*wn3' AS='5*lam*wn3'
+ PS='2*wn3+10*lam' PD='2*wn3+10*lam'
m3b 8 ninm 3 nvss cmosn W=wn3 L=ln3 AD='5*lam*wn3' AS='5*lam*wn3'
+ PS='2*wn3+10*lam' PD='2*wn3+10*lam'
m4b 9 ninp 3 nvss cmosn W=wn3 L=ln3 AD='5*lam*wn3' AS='5*lam*wn3'
+ PS='2*wn3+10*lam' PD='2*wn3+10*lam'
m7 6 nvb2 1 nvss cmosn W=wn7 L=ln AD='5*lam*wn7' AS='5*lam*wn7'
+ PS='2*wn7+10*lam' PD='2*wn7+10*lam'
m5 5 5 nvss nvss cmosn W=wn5 L=ln AD='5*lam*wn5' AS='5*lam*wn5'
+ PS='2*wn5+10*lam' PD='2*wn5+10*lam'
m6 3 5 nvss nvss cmosn W=wn5 L=ln AD='5*lam*wn5' AS='5*lam*wn5'
+ PS='2*wn5+10*lam' PD='2*wn5+10*lam'
m10 5 nvb1 2 2 cmosp W=wp10 L=lp AD='5*lam*wp10' AS='5*lam*wp10'
+ PS='2*wp10+10*lam' PD='2*wp10+10*lam'
m8 6 6 nvdd nvdd cmosp W=wp8 L=lp AD='5*lam*wp8' AS='5*lam*wp8'
+ PS='2*wp8+10*lam' PD='2*wp8+10*lam'
m9 4 6 nvdd nvdd cmosp W=wp8 L=lp AD='5*lam*wp8' AS='5*lam*wp8'
+ PS='2*wp8+10*lam' PD='2*wp8+10*lam'
m21 12 nvb1 8 nvdd cmosp W=wp21 L=lp AD='5*lam*wp21' AS='5*lam*wp21'
+ PS='2*wp21+10*lam' PD='2*wp21+10*lam'
m22 20 nvb1 9 nvdd cmosp W=wp21 L=lp AD='5*lam*wp21' AS='5*lam*wp21'
+ PS='2*wp21+10*lam' PD='2*wp21+10*lam'
m23 12 nvb3 10 nvss cmosn W=wn23 L=ln AD='5*lam*wn23' AS='5*lam*wn23' 
+ PS='2*wn23+10*lam' PD='2*wn23+10*lam'
m24 20 nvb3 11 nvss cmosn W=wn23 L=ln AD='5*lam*wn23' AS='5*lam*wn23' 
+ PS='2*wn23+10*lam' PD='2*wn23+10*lam'
m26 10 12 nvss nvss cmosn W=wn26 L=ln AD='5*lam*wn26' AS='5*lam*wn26' 
+ PS='2*wn26+10*lam' PD='2*wn26+10*lam'
m27 11 12 nvss nvss cmosn W=wn26 L=ln AD='5*lam*wn26' AS='5*lam*wn26' 
+ PS='2*wn26+10*lam' PD='2*wn26+10*lam'
m220 nout 20 nvss nvss cmosn W=wn220 L=ln AD='5*lam*wn220' AS='5*lam*wn220' 
+ PS='2*wn220+10*lam' PD='2*wn220+10*lam'
m221 20 nvdd 21 nvss cmosn W=wn221 L=ln AD='5*lam*wn221' AS='5*lam*wn221' 
+ PS='2*wn221+10*lam' PD='2*wn221+10*lam'
cm nout 21 10p

* Load
cm nout 0 20p
cm nout 0 20k

* Current & voltage sources

ibiasp 30 nvss 12.5u
ibiasn nvdd 40 12.5u

vb1 nvdd nvb1 1.35
vb2 nvb2 nvss 1.3
vb3 nvb3 nvss 1.55

einp ninp ncm input 0 0.5
einm ninm ncm input 0 -0.5

vcm ncm 0 0
vin input 0 -19.585u ac = 1

vdd nvdd 0 1.65
vss nvss 0 -1.65

* Test cards

.dc vin -1m 1m 2u
.ac dec 100 2 100x
.probe ac vdb( nout )

.end
Rail-to-Rail Input Stage, Structure 5 [7]

- Using Hex-Pair Structure to control the tail currents backup pairs

- Basic idea
  - The underlying idea of this structure is similar to structure 4. We utilize main and backup pairs to have a constant $g_m$, and at the same time, a constant total biasing current which will not change with the common mode input voltage. But here we apply a new bias current sensing scheme, which is also utilized in [18].
Rail-to-Rail Input Stage, Structure 5 (cont’d)

- The circuit [7]

Note:
1) Iref1 to Iref6 are with the same value, Iref.
2) All of the P transistors have the same geometry, \((W/L)_P\), for all of the N transistors, \((W/L)_N\), and

\[
K = \frac{1}{2} KP_N \left(\frac{W}{L}\right)_N = \frac{1}{2} KP_P \left(\frac{W}{L}\right)_P
\]
Rail-to-Rail Input Stage, Structure 5 (cont’d)

- Working principle

When the common mode input voltage is in its middle range. Both of the N and P channel devices have sufficient gate bias to operate. In the N-channel circuitry, both M3A and M4A contribute signal current, with a transconductance set by half of the total current available, i.e., Iref. The other half of the tail current, also Iref, is diverted to M3B and M4B, since all of the N transistors are of the equal size, and have the same mean gate source voltage. This diverted current in turn draws the tail current Iref6 away from the P channel pair M1C and M2C, switching them off. On the P side, M1A and M2A contribute signal current. And the current of M1B, M2B draws away the tail current of M3C and M4C.

Hence, the total signal output is supplied by 4 transistors, M1A, M2A, M3A and M4A. The transconductance is 2gm, and the total tail current available is 2Iref.
When the common mode input voltage is close to $V_{DD}$, None of the P channel transistors have sufficient gate source voltage to remain active. The current sources supplying M1A, M1B, M2A, and M2B collapse and turn off. M3C and M4C become active and contribute signal current to the output. Hence, the total signal output is again supplied by 4 transistors, M3A, M4A, M3C and M4C. The total transconductance is $2g_m$, and the total tail current available is still $2I_{ref}$. 
When the common mode input voltage is close to $-V_{SS}$. None of the N channel transistors have sufficient gate source voltage to remain active. The current sources supplying M3A, M3B, M4A, and M4B collapse and turn off. M1C and M2C become active and contribute signal current to the output. Hence, the total signal output is again supplied by 4 transistors, M1A, M2A, M1C and M2C. The total transconductance is $2g_m$, and the total tail current available is still $2I_{ref}$. 
Rail-to-Rail Input Stage, Structure 5 (cont’d)

- Transconductance vs. input common mode voltage

- Similar to constant-gm input stage structure 4, there are also 2 bumps on the gm curve, where the transconductance is 20% greater than its nominal value. The bumps are at take-over regions.

- By similar analysis we can determine the maximum value of the total transconductance is

\[ gm_T = \sqrt{2K_{Iref}} (\sqrt{2} + 1) = 2.414\sqrt{2K_{Iref}} \]

which is about 20% larger than its nominal value \(2\sqrt{2K_{Iref}}\).
Rail-to-Rail Input Stage, Structure 6 [8][9]

- Using Maximum/Minimum selection circuit
- The basic idea
  - From previous analysis, we know that, when the common mode voltage drives the tail current transistor out of saturation region, the tail current of a differential pair decreases dramatically with the common mode voltage. As shown in the following figure.
  
  - The differential pair, whichever it is N pair or P pair, with the larger current should be working properly. We just try to choose the pair with larger working current, and discard the output of another pair.
Rail-to-Rail Input Stage, Structure 6 (cont’d)

- The block diagram
Rail-to-Rail Input Stage, Structure 6a (cont’d)

- Maximum Current Selection Circuit

  - When $I_{in1} > I_{in2}$, M2 and M3 try to mirror $I_{in1}$, but as $I_{in2} < I_{in1}$, there is no enough current for M3 to sink, M3 will work in Ohmic region and its $V_{DS}$ is very small. M4 and M5 are off. So $I_{out} = I_{in1}$
  
  - When $I_{in2} > I_{in1}$,
    
    \[
    I_{D,M2} = I_{D,M3} = I_{in1}, \\
    I_{D,M4} = I_{D,M5} = I_{in2} - I_{in1}. \\
    I_{out} = I_{D,M5} + I_{D,M3} = I_{in1} + (I_{in2} - I_{in1}) = I_{in2}
    \]
Rail-to-Rail Input Stage, Structure 6a (cont'd)

- The whole input stage

Please notice that wires with = are connected to Maximum Current Selection I, and the wires with ≈ are connected to Maximum Current Selection II.
Rail-to-Rail Input Stage, Structure 6a  
( cont’d )

• Working Principle
  – Please notice that if we apply a positive differential voltage to the inputs $V_{i+}$ and $V_{i-}$, the currents of $M_1$ (P type) and $M_4$ (N type) will decrease, and the currents of $M_2$ (P type) and $M_3$ (N type) will increase. We apply the current of $M_2$ and mirrored current of $M_3$ to Maximum Selection Circuit I, and current of $M_1$ and the mirrored current of $M_4$ to Maximum Selection Circuit II.
  – When the common mode input voltage is close to $V_{dd}$, the tail current of the P input pair decreases, the maximum selection circuits conduct the drain currents of N pair to the outputs.
  – When the common mode input voltage is close to $-V_{ss}$, the tail current of the N input pair decreases, the maximum selection circuits conduct the drain currents of P pair to the outputs.
  – At the outputs, we get the larger currents of the 2 input pairs, and hence the larger $g_m$. 
Rail-to-Rail Input Stage, Structure 6a (cont’d)

- Transconductance vs. input common mode voltage
Rail-to-Rail Input Stage, Structure 6b (cont’d)

- There is another configuration which utilizes folded cascode circuit and minimum selection circuit to get the maximum gm
  - As in the folded cascoded shown in the circuit below, if $I_{in}$ is at its maximum value, we will get a minimum $I_{out}$. So with this folded cascode circuit, we cannot use maximum selection circuit, instead, we should use minimum selection circuit.
  - Why folded cascode circuit?
  - The key advantage of this configuration over the previous one is that it has a wider common mode range! If it is properly biased, we can get a common mode range which may exceed the power supply rails!
Rail-to-Rail Input Stage, Structure 6b (cont’d)

• The minimum selection circuit
  – As shown in the right circuit, all N transistors are with the same geometry, and P transistors are with the same geometry.
  – If $I_{in2} < I_{in1}$, $I_{D,M5} = I_{D,M6} = I_{D,M7} = I_{in2}$, M2 works in ohmic region, and M3 and M4 are off. $I_{out} = I_{D,M7} = I_{in2}$.
  – If $I_{in1} < I_{in2}$, $I_{D,M5} = I_{D,M6} = I_{D,M7} = I_{in2}$, $I_{D,M1} = I_{D,M2} = I_{in1}$, $I_{D,M3} = I_{D,M4} = I_{in2} - I_{in1}$, $I_{out} = I_{D,M7} - I_{D,M4} = I_{in2} - (I_{in2} - I_{in1}) = I_{in1}$.
Rail-to-Rail Input Stage, Structure 6b (cont’d)

- The input stage with folded cascode and minimum selection circuit
Rail-to-Rail Input Stage, Structure 7 [10]

- Using electronic zener diode to keep $V_{GSn} + |V_{GSp}|$ constant
- Basic idea
  - We have know that to have a constant $g_m$, we can use square-root circuit to keep $(\sqrt{I_P} + \sqrt{I_N})$ constant, -- is there any other way to do that?

- Please observe the complementary input stage
  
  \[ V_{i2} = V_1 - V_2 = V_{GSN} + |V_{GSP}| \]
  
  \[ V_{GSN} = \sqrt{\frac{I_N}{2K}} + V_{TN} \quad \text{and} \quad |V_{GSP}| = \sqrt{\frac{I_P}{2K}} + |V_{TP}| \]

  where \[ K = \frac{1}{2} KP_N \left( \frac{W}{L} \right)_N = \frac{1}{2} KP_P \left( \frac{W}{L} \right)_P \]

  so

  \[ (\sqrt{I_P} + \sqrt{I_N}) = \sqrt{2K} (V_{GSN} + |V_{GSP}| - V_{TN} - |V_{TP}|) \]
  
  \[ = \sqrt{2K} (V_{i2} - V_{TN} - |V_{TP}|) \]
Rail-to-Rail Input Stage, Structure 7 (cont’d)

– To keep \((\sqrt{I_P} + \sqrt{I_N})\) constant is equivalent to keep \(V_{GSN} + |V_{GSP}|\) constant if the transistors work in strong inversion region!

– We can get this conclusion by another way

\[
\begin{align*}
    gm_T &= gm_N + gm_P \\
    gm_N &= 2K(V_{GSN} - V_{TN}) \quad \text{and} \quad gm_P = 2K(|V_{GSP}|-|V_{TP}|) \\
    \text{so} \quad gm_T &= gm_N + gm_P = 2K(V_{GSN} + |V_{GSP}| - V_{TN} - |V_{TP}|) \\
    \text{To get a constant Gm, we should keep } V_{GSN} + |V_{GSP}| \text{ constant.}
\end{align*}
\]

– Instead of controlling the tail current of the differential pair to have a constant \(gm_T\), we can keep \(V_{GSN} + |V_{GSP}|\) constant!

– This idea is shown in the block circuit diagram in the following.
Rail-to-Rail Input Stage, Structure 7 (cont’d)

- The circuit showing the principle

Please notice that the floating voltage source $V_z$ keeps $V_{GSN+}|V_{GSP}|$ constant, the value of $V_z$ is defined by

$$V_z = \frac{g_{mT}}{2K} + V_{TN} + |V_{TP}|$$
Rail-to-Rail Input Stage, Structure 7 (cont’d)

- Transconductance vs. input common mode voltage of the circuit in previous slide (with ideal voltage source Vz)

![Graph showing transconductance vs. input common mode voltage]

- Line with a label: With gm-control of Vz
- Dashed line with a label: Without gm-control

Vicm vs. Gm with Vdd and -Vss as reference points.
Rail-to-Rail Input Stage, Structure 7 (cont’d)

- One implementation with a simple electronic zener of 2 dioded connected CMOS FETs [10]

In this circuit, the voltage source Vz is replaced by 2 diode connected MOS transistors.

The small and large signal behavior of this electronic zener deviates from that of an ideal voltage source, which may introduce gm control error shown in next slide.
Rail-to-Rail Input Stage, Structure 7 (cont’d)

- Transconductance vs. input common mode voltage

Because of the non-ideality of the diode-connected transistors from ideal voltage sources, there are 2 dips in the transisconductance curve.
Rail-to-Rail Input Stage, Structure 7 (cont’d)

- A more precise electronic zener implementation [10]
Rail-to-Rail Input Stage, Structure 7  ( cont’d )

- Working Principle
  - In this circuit, the electronic zener is implemented by transistors M5-M8, Mb3, and Mb6. Mb3 and Mb6 are current sources.
  - As the load of M7 is a current source, and M5, M6, M7 and M8 form a feedback loop which defines the current through M7. Please note that M5 and M7 are current mirrors, $I_{D,M5} = I_{D,M7}$. So the current through M5 and M6 is constant. M5-M8 loop is equivalent to a zener with very low resistance. By small signal analysis, we can obtain the conductance for the electronic zener is

\[
g_{equ} = \frac{g_{m5} g_{m6}}{g_{m5} + g_{m6}} \left( \frac{g_{m7} g_{m8}}{g_{o7} + g_{o, Mb6}} \right) + 1
\]

which is \left( \frac{g_{m7} g_{m8}}{g_{m5} g_{o7} + g_{o, Mb6}} + 1 \right) times larger than that the simple zener implementation.
Rail-to-Rail Input Stage, Structure 7 (cont’d)

- Transconductance vs. input common mode voltage

![Graph showing transconductance vs. input common mode voltage with and without gm-control of modified zener. The graph shows a smooth transition from -Vss to Vdd with the blue line representing 'With gm-control of modified zener' and the red dashed line representing 'Without gm-control'.]
Rail-to-Rail Input Stage, Structure 8 [11]

- Using DC shifting circuit to change the input DC level
- Basic idea

- We may notice that there is an overlap between \( g_{mN} \) and \( g_{mP} \), so in the middle of the common mode voltage, the transconductance is doubled.

- How about shift one of the \( g_{mN} \) and \( g_{mP} \) curve? And let the transition regions of \( g_{mN} \) and \( g_{mP} \) come together, so that the total transisconductance will be nearly constant among the common mode input range.

- Level shift can be implemented by common source voltage follower. We can change the shift level by altering the bias current \( I_b \).
Rail-to-Rail Input Stage, Structure 8 (cont’d)

- The circuit [11]

Note: 1) M5 and M6 are level-shifting transistors
2) The voltage shifted by M5 and M6 can be altered by changing Ib.
Rail-to-Rail Input Stage, Structure 8 (cont’d)

• Working principle
  – The input voltages are shifted by M5, M6 by $|V_{\text{GS,M5,M6}}|$ towards the positive power supply rail, so the transition region for $g_{mP}$ is shifted by the same value towards the negative power supply rail.
  – The transition region of $g_{mN}$ and $g_{mP}$ overlap and we can get a constant $g_{m}$ over the common mode range.
Rail-to-Rail Input Stage, Structure 8 (cont’d)

- Characteristics
  - We can obtain very small gm variation (±5%) if the DC shift level is tuned well [11].
  - This circuit structure is sensitive to the power supply changes and $V_T$ variations, but we can add some auto-bias circuit to overcome this problem.
Experimental amplifier behavior in unity-gain feedback configuration: (a) dc transfer characteristic, (b) transient response.
## Summary and Comparison

<table>
<thead>
<tr>
<th>Case</th>
<th>Principle</th>
<th>$\Delta gm$</th>
<th>Slew Rate</th>
<th>CMRR</th>
<th>Advantage</th>
<th>Limitations</th>
</tr>
</thead>
</table>
| 1    | $I_N + I_P = const$ [1][2][6] | N/A for weak inversion  
40% if in strong inversion | Constant | 56dB@10Hz,  
52dB@100KHz, measured in [2] | Small gm variation (6%) in weak inversion operation | Only work well in weak inversion, cannot be used in high speed application |
| 2    | $\sqrt{I_N} + \sqrt{I_P} = const$ [3][16] | -12% +6% (simulated in this presentation)| $\sqrt{2}$ times variation | 80 dB / 53 dB (measured in [3]) | Depends on quadratic characteristics of MOSFETs, which is not exactly followed for short channel transistors in sub-micron processes |
| 3    | 4 times $I_N$ or $I_P$ when only one pair operates [3][4][6] | +15% systematic gm variation | 2 times variation | 70dB / 43 dB (measured in [4]) | Somewhat simple |
| 4    | Current switch, backup pairs [5] | +20% systematic gm variation | Constant | N/A | Constant slew rate | Systematic gm deviation of 20% even for ideal MOSFETs with quadratic characteristics |
| 5    | 6-pair structure, back pairs [7] | +20% systematic gm variation (analytical)  
±10% (measured in [7]) | Constant | N/A | Constant slew rate | Same with Case 4 |
| 6    | Max/min selection [8][9] | 7% (simulated [9])  
5% (strong inversion, measured [8])  
20% (weak inversion, measured [8]) | Constant | N/A | Somewhat complex | |
| 7    | Electronic zener [10] | 8% (measured) | 80 dB / 43 dB (measured in [10]) | Same with Case 2 |
| 8    | Level shift [11] | ±4% after tuning  
13% before tuning (measured) | ≥80 dB (DC) (measured in [11]) | Simple | Gm variation sensitive to $V_T$ variation and power supply voltage change |
References


References (cont’d)


References (cont’d)


